

Study Guide

Number Relation Problems 02/29/2012

Number Relation Problems

Number relation problems involve sentences that must be translated into equations.

To translate sentences, review the following phrase/number equivalences:

If x is equal to 4, then $x = 4$

If the sum of 2x and 2y is 23, then $2x + 2y = 23$

If 3 is less than twice y, then $2y > 3$

If 5x decreased by y is more than 2y, then $5x - y > 2y$

If the result of 7 more than 3 times x is y, then $3x + 7 = y$

Example: One number is 2 less than another number. If twice the larger number is decreased by 3 times the smaller number, the result is 20.

Set Up Equations	
Step 1:	$x + 2 = y$
Step 2:	$2y - 3x = 20$

Solve for "x"	Solve for "y"
Step 3: $2(x + 2) - 3x = 20$	Step 8: $2y - 3(-16) = 20$
Step 4: $2x + 4 - 3x = 20$	Step 9: $2y + 48 = 20$
Step 5: $-x + 4 = 20$	Step 10: $2y = -28$
Step 6: $-x = 16$	Step 11: $y = -14$
Step 7: $x = -16$	

Check Your Work	
$x + 2 = y$	$2y - 3x = 20$
$(-16) + 2 = -14$	$2(-14) - 3(-16) = 20$
$-14 = -14$	$-28 - 48 = 20$
	$20 = 20$

Step 1: Translate the first sentence in the problem into the first equation.

Let x and y represent the unknown numbers, with y representing the larger number and x representing the smaller number.

Step 2: Translate the second sentence in the problem into the second equation.

Use x and y as in the first equation, substituting them into their respective locations in the equation.

Step 3: Substitute $x + 2$ for y in the second equation.

Step 4: Distribute the 2 across $(x + 2)$.

Step 5: Combine the similar terms.

Step 6: Subtract 4 from both sides.

Step 7: Divide each side by -1 to find the value of x.

Step 8: Using $x = -16$, substitute for x in the second equation.

Step 9: Multiply -3 and -16.

Step 10: Subtract 48 from both sides.

Step 11: Divide each side by 2.

Answer: $x = -16$ and $y = -14$

As always, check the solutions by substituting both equations with $x = -16$ and $y = -14$.

